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PADDING ORACLES

TTM4205 – Lecture 13

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Contents

Padding Oracles

Recall: RSA Encryption

RSA Padding Schemes

The Bleichenbacher Attack

Improved Bleichenbacher Attack

RSA Padding Oracle Mitigations



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Reference Material

These slides are based on:

- The referred papers in the slides
- JPA: parts of chapter 10
- DW: parts of chapter 6



By this we mean, on a high level, an API that allows an adversary to check if some input is correctly formed.

We limit ourselves to input with a particular padding.

A limited version of the protocol APIs from last week.



Padding Oracles

We will look at symmetric and asymmetric padding schemes:

- more in depth on CBC mode (last time)
- extension attacks against hashing (last time)
- padding attacks against RSA scheme (today)

Several of which are relevant to the weekly problems.

We will also look at some mitigations to these issues.



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The plain RSA encryption scheme works as follows:

KGen:

Samples primes *p* and *q* of appropriate size and entropy

- Use fixed e and compute $d \equiv e^{-1} \mod \operatorname{lcm}(p-1, q-1)$
- Output the key pair $pk = (e, n = p \cdot q)$ and sk = (d, p, q)



The plain RSA encryption scheme works as follows:

Enc:

- Takes as input a message m and public key pk = (e, n)
- Computes the ciphertext $c \equiv m^e \mod n$ and outputs c



The plain RSA encryption scheme works as follows:

Dec:

- Takes as input a ciphertext c and secret key sk = (d, p, q)
- Computes the message $m \equiv c^d \mod p \cdot q$ and outputs m





Question: Why is not the textbook RSA scheme secure?



The following things make the RSA scheme insecure:

- It is not randomized and hence not even CPA secure
- Given a ciphertext you can search for the message
- High-entropy messages still gives the same ciphertext
- The Jacobi symbol of m and c will be the same

Solution: structured, but randomized padding



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Let *n* be of *k* bytes. Given a message *m* of $\ell \le k - 11$ bytes, the padded messages \overline{m} of length *k* bytes is constructed as follows: 00 02 {at least 8 non-zero random bytes} 00 {*m*}.

Quite simple, not proven secure, not secure in practice...



A bad couple of years for the cryptographic token industry



Figure: https://blog.cryptographyengineering.com/2012/06/2 1/bad-couple-of-years-for-cryptographic



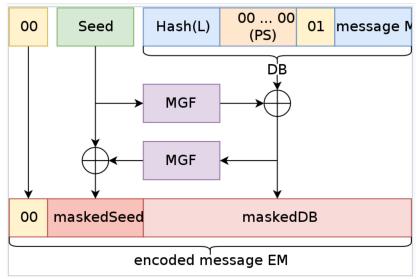


More complex, proven secure, what you should use:

- Let *n* be of *k* bytes and message *m* be of ℓ bytes.
- ▶ Let MGF and Hash be hash functions with output *h* bytes.
- Let *L* be a label (which can be set to the all zero string)
- ► Let seed be an ephemeral random string of *h* bytes.
- Let PS be a all zero string of length $k \ell 2h 2$ bytes.



OAEP



Optimal Asymmetric Encryption — How to Encrypt with RSA

Mihir Bellare* Phillip Rogaway[†]

November 19, 1995

Figure: https://cseweb.ucsd.edu/~mihir/papers/oaep.pdf



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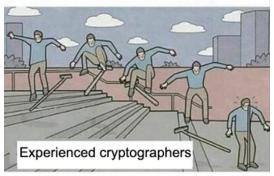
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New cryptographers





However, many implementations (still) use RSA-PKCS#1v1.5 or similar padding schemes (note that this is version 1.5).

Recall: $00\ 02$ {at least 8 non-zero random bytes} $00\ \{m\}$.

Question: Assuming no integrity check of RSA ciphertexts, how could you attack this scheme?





• Recall that RSA is homomorphic: $\bar{m}^e \cdot r^e \equiv (\bar{m} \cdot r)^e \mod n$.



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- Then we learn that unknown \bar{m} times r is valid encoding.
- We know that if valid then $2 \cdot 2^{8(k-2)} \leq \overline{m} \cdot r < 3 \cdot 2^{8(k-2)}$.
- Repeat for fresh values r until we have a unique \bar{m} left.



Chosen Ciphertext Attacks Against Protocols Based on the RSA Encryption Standard PKCS #1

Daniel Bleichenbacher

Bell Laboratories 700 Mountain Ave. Murray Hill, NJ 07974 E-mail: bleichen@research.bell-labs.com

Figure: https://spar.isi.jhu.edu/~mgreen/bleichenbacher.pdf



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- **2.** Trim the randomness to a specific interval [a, b]
- 3. Parallelization and threading and pre-computation
- 4. Adapt based on how strict padding checks are





The efficiency depends on how strict the padding check is:

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- **4.** TFT: same as above, but 'ok' even if there are no zeros after the first byte.
- **5.** TTT: padding is 'ok' as long as it starts with 0×0002 .



Oracle	Original algorithm		Modified algorithm			
	Mean	Median	Mean	Median	Trimmers	Mean skipped
FFF	-	-	18 040 221	12 525 835	50 000	7 321
FFT	$215 \ 982$	$163 \ 183$	49 001	14 501	1 500	65 944
FTT	$159 \ 334$	111 984	39 649	11 276	2000	61 552
TFT	39 536	24 926	10 295	4 014	600	20 192
TTT	38 625	22 641	9 374	3 768	500	18 467

Table 1: Performance of the original and modified algorithms.

Figure: https://eprint.iacr.org/2012/417.pdf



Efficient Padding Oracle Attacks on Cryptographic Hardware*

Romain Bardou¹, Riccardo Focardi^{2**}, Yusuke Kawamoto^{3***}, Lorenzo Simionato^{2†}, Graham Steel^{4***}, and Joe-Kai Tsay^{5***}

¹ INRIA SecSI, LSV, CNRS & ENS-Cachan, France
² DAIS, Università Ca' Foscari, Venezia, Italy
³ School of Computer Science, University of Birmingham, UK
⁴ INRIA Project ProSecCo, Paris, France
⁵ Department of Telematics, NTNU, Norway

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Use OAEP padding for encryption



- Use OAEP padding for encryption
- Encrypt-then-Authenticate



- Use OAEP padding for encryption
- Encrypt-then-Authenticate
- Do not use RSA for encryption



Questions?

